

Motivation and Background

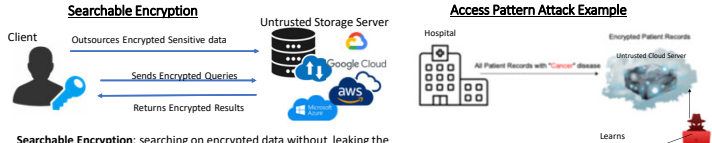
Scientific Data Examples

- Genomics
- Astronomy
- Climate Science
- User locations
- ...

Data Outsourcing as a solution for data owners



Privacy Issues of Sensitive Data Outsourcing: Outsourcing data to third-party servers requires trusting them not to inspect or leak it, a guarantee they often cannot provide.



Searchable Encryption: searching on encrypted data without leaking the database contents and the query to the server

Oblivious RAM (ORAM): Hides Access patterns

A compiler that Re-randomize data locations after every operation



- Server sees encrypted block B accessed → B contains cancer records
- Result size → number of cancer patients

Organizing Records for Retrieval in Multi-Dimensional Range Searchable Encryption[1]

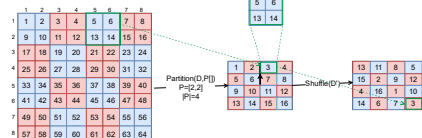
In this research we Focus on Multi-dimensional Range queries and Security and efficiency of the record retrieval.

Data Partitioning groups tuples into parts: requesting any tuple retrieves its whole part, hiding which tuple was of interest. We compare two strategies.

Query Geometry: We test four query shapes (isotropic, bisected, gradual, outlier) and measure how shape affects retrieval cost and leakage.

Secure Data Retrieval Methods to Hide the Access Pattern: Shuffling randomizes record positions during setup or retrieval. ORAM write-backs and shuffling happens with every query.

Slab-Wise Shuffling (SLW-shuffle)



Security Evaluation: Leakage Metrics

Size	Query Type	Shuffling Technique	Avg. STD	Parts
[1,2]	Isotropic	RW-shuffle	209	71
		DRW-shuffle	82	68
		SLW-shuffle	87	92
		Terminus	209	71
[1,2,3]	Avg = 150000	RW-shuffle	259	135
	STD = 207000	DRW-shuffle	85	69
		SLW-shuffle	74	74
		Terminus	259	135
[1,2,3,4]	Avg = 120000	RW-shuffle	295	151
	STD = 180000	DRW-shuffle	62	48
		SLW-shuffle	42	30
		Terminus	295	151
[1,2,3,4,5]	Avg = 40900	RW-shuffle	291	91
	STD = 30000	DRW-shuffle	19	8.8
		SLW-shuffle	74	23
		Terminus	291	91
[1,2,3,4,5,6]	Outlier Max	RW-shuffle	191	91
	Avg = 730	DRW-shuffle	40	14
	STD = 710	SLW-shuffle	63	43
		Terminus	191	91

H: ORAM (Volume Leakage) Lower values: stronger security
 Avg: Shuffling (Access Pattern Leakage) Lower Values: stronger security/better Efficiency
 Finding: SLW-shuffle is more secure and efficient than DRW for nearly all query shapes. DRW only wins when the query is narrow on the indexed dimension and wide on the others (outlier-min).

SPANNS: Scalable Privacy-Preserving Approximate Nearest Neighbor Search

K-ANN Search: Returns the k nearest points to a query in a high-dimensional vector database. Powers RAG in LLMs, recommenders, ML retrieval.

HNSW Graph[7] is the fastest ANN algorithm at high accuracy (recall@k): a multi-layer graph traversed by greedy search from an entry point. Search complexity is poly-logarithmic.

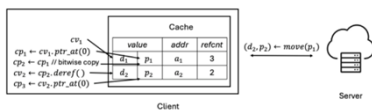
Goal: Oblivious K-ANN search that protects data, queries, results, and access patterns against an untrusted server. Prior approaches leak information, sacrifice accuracy, or fail to scale [8]. We present an oblivious HNSW-based K-ANN algorithm with high recall and scalability to larger dataset sizes for high-dimensional vector databases.

Optimization: 1-D splay tree with dummy nodes handles high in-degree HNSW nodes.

Oblivious Single Access Machine(OSAM)[9]: a weakening of ORAM that improves efficiency for pointer-chasing programs, including graph-based data structures.

Implementation: HNSW partitioned into subgraphs, each stored in one OSAM block; blocks maintain pointers to neighbors.

OSAM Cache Implementation

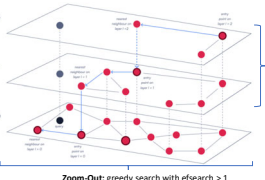


HNSW Oblivious Encrypted Search

HNSW Plain Text Search

Two phase Search : Zoom-in and Zoom-out

- 1- greedy search(BFS) in each layer to find the closest neighbor (efSearch-1).
- 2- Start search starting from the found closest node in the next layer and continue until the l=1.



Zoom-out: greedy search with efSearch > 1

SPARQ: Scalable Privacy-Preserving Aggregate Range Queries[2]

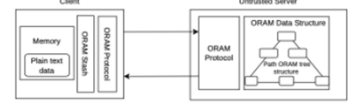
SPARQ enables aggregate range queries (SUM, AVG, COUNT, MIN, MAX, STDDEV) on encrypted multi-dimensional data without revealing the query, the data, or access pattern. Prior approaches require storage proportional to the domain size (impractical for large-scale sparse data) or use FHE (computationally expensive). We use oblivious multi-dimensional segment trees: storage scales with distinct values per dimension, not the domain.

Result: 10x to 10¹⁰x less storage and under 1.2 s server-side latency on a 32-thread machine for our largest 3D dataset.

ORAM-based Architecture

Precompute and store in the ORAM Storage Format

- Multidimensional Segment tree
- Each node of the tree → (node_id, value, meta) in ORAM
- Calculate the aggregation over a range by
- Traversing the tree by retrieving data from the ORAM
- Interactive algorithm

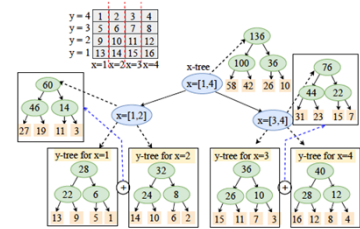


Storage Efficiency

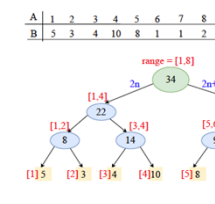
dataset	ST Max Act	Key Value Based					FHE %FCAR
		SUM	Min	Quasi	Lin	R. Cover	
books	4.2	5.9	8.1	7.8	5.9	5.9	4.0
gonalla	7.9	7.7	9.0	13.4	7.0	7.9	7.1
Spitz	6.2	4.6	6.0	4.7	6.5	6.0	6.1
call	6.6	5.5	6.0	7.7	8.5	6.0	6.6
gonalla	7.2	5.7	10.8	13.0	10.0	9.8	9.8
gonalla	8.1	6.1	11.9	13.2	11.9	10.9	10.9
synthetic	7.2	6.8	6.6	8.4	12.0	6.7	8.4
synthetic	7.2	6.8	12.9	14.3	12.3	12.0	12.0
synthetic	6.6	6.6	12.9	14.3	12.3	12.0	12.0
ml	6.3	5.2	5.4	7.3	7.2	5.4	6.9
gonalla	6.4	5.7	6.0	8.0	8.7	6.0	7.8
synthetic	7.1	7.1	18.0	21.4	18.0	18.0	18.0
synthetic	8.1	7.6	18.0	21.4	21.0	21.0	13.1

Table 1: Key-value based storage format. For Map and tree based solutions we list the number of items in the M. For the EMT approach which relies on an MM we list the number of stored items when padded to the maximum number of items associated with any key. ST Max is the size of segment tree size based on $H_{2^k}(2^k - 1)$. ST Act is the size of the segment tree which is stored in OMAP in practice per dataset based on the experiments.

2-d Segment tree



1-d Segment tree



Cryptography Efficiency

dataset	Oblivious Segment Tree			Discretized Prefix Array		
	Setup	Rd Search	Par. Size	BW Setup	Search Size	Size BW
Books ID	15	15	0.05	0.01	17.0MB	171.0KB
gonalla ID	1819	25	2.1	0.02	17.8MB	507.0KB
Spitz ID	49	23	0.55	0.02	690KB	3.4MB
call ID	413	23	0.78	0.02	560.0MB	4.2MB
gonalla 2D	756	26	1.1	0.024	1.1GB	5.7MB
gonalla 2D	2229	29	1.7	0.029	2.2GB	8.1MB
synthetic 2D-2018-ap	1584	25	3.2	0.027	18GB	5.7MB
synthetic 2D-2018-ap	6127	23	1.7	0.021	4.4GB	4.3MB
ml 3D	290	22	2.24	0.022	278.5MB	17.3MB
gonalla-3D	706	24	3.45	0.027	1.1GB	18.8MB
synthetic 3D-128	23437	25	8.37	0.035	18GB	31MB
synthetic 3D-256	9718	28	21.92	0.046	71GB	54MB

Table 2: Measuring the ORAM performance over 1000 sample aggregation queries. Rd is the average access depth plus one. Par. is the sum of the (average) of the maximum ORAM retrieval at each depth. Setup, search, and Par. are setup time, search time, and parallel search time in seconds.

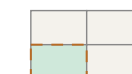
Coordinating Structure of Shuffling and Indexing in Encrypted Range Queries

Approach. Coordinate index and shuffle structures in encrypted multi-dimensional range search. **Result.** Reduced retrieval overhead and lower leakage to the untrusted server.

Core Idea

- Encrypted range queries use range trees or quadtrees as indexes.
- Independent shuffling causes excess accesses and leaks query geometry.
- Like-structured shuffling: align record partitions to the index's geometry.

Tree shuffle + tree index partitions align with query range



1 page fetched

12 relevant, 3 false positives

Grid shuffle + tree index partitions ≠ query range



4 pages fetched

5 relevant, 10 false positives

relevant record (green), false positive (grey)

Cache Saving Write-Back We propose write-back schemes which prioritizes keeping likely-reused data present, without leaking measurably more to the server.

System-Wide Leakage

- Standard model: query tokens, response sizes.
- Our model: full retrieval trace — fetched pages, write-back timing, shared record overlap.

Policies safe in isolation can leak under the full trace.

We evaluate how index structure, query geometry, and write-back policies affect storage, query cost, communication, and four leakage channels: retrieval patterns, page co-occurrence, volume, and timing.

Main Takeaway Aligning index and shuffle structures cuts redundant retrieval, lowers storage pressure, and weakens leakage. It offers a practical middle ground: much stronger security than naive shuffling, but with far less overhead than full ORAM.

References

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